

Fubini's Theorem- HW Problems

1. Evaluate $\iiint_W (x^2 + y^2 + z^2) dx dy dz$, where W is the solid cylinder given by $x^2 + y^2 \leq 2$, $-2 \leq z \leq 3$, by changing to cylindrical coordinates:

$$x = r \cos \theta, \quad y = r \sin \theta, \quad z = z.$$

Show how you calculated the jacobian.

2. Evaluate $\iiint_W \frac{dx dy dz}{(x^2 + y^2 + z^2)^{\frac{3}{2}}}$, where W is the solid bounded by

$$x^2 + y^2 + z^2 = a^2 \quad \text{and} \quad x^2 + y^2 + z^2 = b^2, \quad 0 < b < a.$$

change to spherical coordinates:

$$x = \rho \cos \theta \sin \varphi, \quad y = \rho \sin \theta \sin \varphi, \quad z = \rho \cos \varphi.$$

Show how you calculated the jacobian.