

## Continuity of Measure- HW Problems

1. Define  $E\Delta F = (E\sim F) \cup (F\sim E)$ . Let  $E = (0,1)$ ,  $F = (-\frac{1}{2}, \frac{1}{2})$ , and  $G = (\frac{1}{4}, \frac{5}{4})$ . Find  $E\Delta F$ ,  $F\Delta G$ , and  $E\Delta G$ .
2. Suppose  $E, F$ , and  $G$  are measurable subsets of  $[0,1]$  and  $m(E\Delta F) = m(F\Delta G) = 0$ . Prove that  $m(E\Delta G) = 0$ .
3. Show that the finite additivity of the Lebesgue measure with the continuity of measure implies countable additivity of the Lebesgue measure.